

Charles' Law (Temp.-Vol. Relationship)

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For a fixed mass of a gas [m] at constant P, volume of a gas increases on increasing temperature and decreases on cooling.

BL \rightarrow $P \propto 1/V$
 $\uparrow V \propto T \uparrow$
for a fixed mass of gas at constt. P
T incr and V incr
T decr and V decr

They found that for 1°C rise in temperature, volume of a gas increases by $1/273.15$ [new volume, V_t] from the original volume [V_0] of the gas that is kept at 0°C .

New Volume = $V_1 = V_0 + 1/273.15$ at increase of 1°C rise

Thus if the volumes of the gas at 0°C is V_0 and at 1°C rise = $t^\circ\text{C}$ is V_t respectively, then

$$\begin{aligned} V_t &= V_0 + \frac{t}{273.15} V_0 \\ \Rightarrow V_t &= V_0 \left(1 + \frac{t}{273.15} \right) \\ \Rightarrow V_t &= V_0 \left(\frac{273.15 + t}{273.15} \right) \end{aligned} \quad (5.6)$$

If we write $T_t = 273.15 + t$ and $T_0 = 273.15$

$$\begin{aligned} V_t &= V_0 \left(\frac{T_t}{T_0} \right) \\ \Rightarrow \frac{V_t}{V_0} &= \frac{T_t}{T_0} \end{aligned} \quad (5.7)$$

Note

$0^\circ\text{C} = 273.15\text{K}$ = Kelvin temperature scale or Absolute temperature scale
or Thermodynamic scale